

The Pythagorean Theorem

SOL G.8

Learning Target: By the end of class today, I will be able to solve real world problems to classify triangles and find missing sides of right triangles using the Pythagorean theorem by solving problems collaboratively as a class and answering 4 out of 5 questions correctly on an exit ticket.

Essential Questions: G.8

- How is the Pythagorean Theorem derived and what is significant about its derivation?
- How are ratios used to solve for unknown lengths of sides in a right triangle?

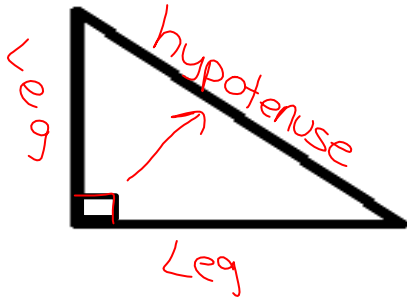
Today's Agenda

- ✓ DO NOW
- ✓ Intro to Right Triangles
- ✓ Pythagorean Theorem
- ✓ Workertown Map Activity
- ✓ Exit Ticket

CODE YELLOW

Vocabulary

Right Triangle – A triangle with one right angle



Hypotenuse
the longest side
of a right triangle

The Pythagorean Theorem

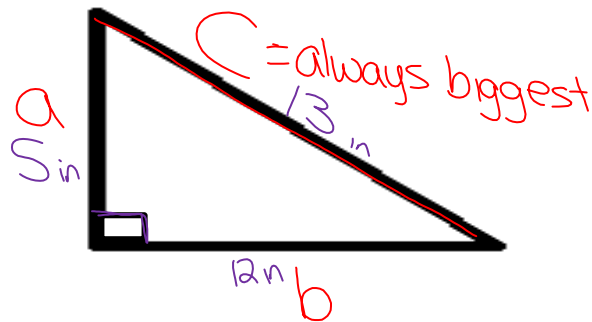
$$c^2 = a^2 + b^2$$

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The Pythagorean Theorem

$$c^2 = a^2 + b^2$$

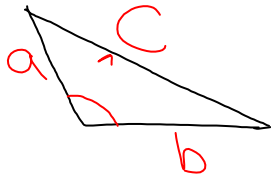
$$13^2 = 5^2 + 12^2$$



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Other types of triangles:

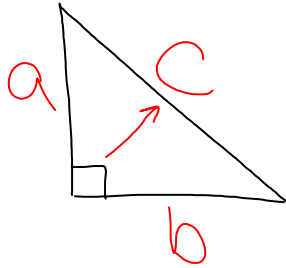
Obtuse



$$c^2 > a^2 + b^2$$

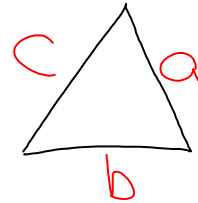
greater

Right



$$c^2 = a^2 + b^2$$

Acute



$$c^2 < a^2 + b^2$$

less

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Use the following sets of given side lengths to determine if the triangle is a right, obtuse, or acute triangle.

1) 7, 10, 12

$$c^2 = a^2 + b^2$$

$$12^2 = 10^2 + 7^2$$

$$144 = 100 + 49$$

$$144 < 149 \quad \text{acute}$$

2) 4, 8, 9

$$c^2 = a^2 + b^2$$

$$9^2 = 4^2 + 8^2$$

$$81 = 16 + 64$$

$$81 > 80 \quad \text{obtuse}$$

3) 4, 5, 3

$$c^2 = a^2 + b^2$$

$$5^2 = 4^2 + 3^2$$

$$25 = 16 + 9$$

$$25 = 25 \quad \text{right}$$

CODE GREEN

Use the following sets of given side lengths to determine if the triangle is a right, obtuse, or acute triangle.

1) 6, $\overset{c}{10}$, 8

$$100 = 100$$

right

2) 3.4, 6.3, $\overset{c}{7.1}$

$$50.41 < 51.25$$

acute

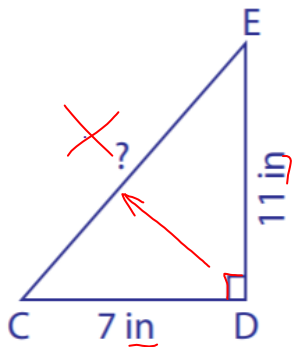
3) 4, 8, $\overset{c}{11}$

$$121 > 80$$

obtuse

CODE YELLOW

Solving for missing sides:



$$c^2 = a^2 + b^2$$

$$x^2 = 11^2 + 7^2$$

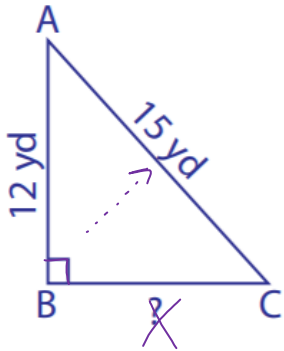
$$x^2 = 121 + 49$$

$$\sqrt{x^2} = \sqrt{170}$$

$$x = 13.04$$

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Solving for missing sides:



$$c^2 = a^2 + b^2$$

$$15^2 = X^2 + 12^2$$

$$225 = X^2 + 144$$

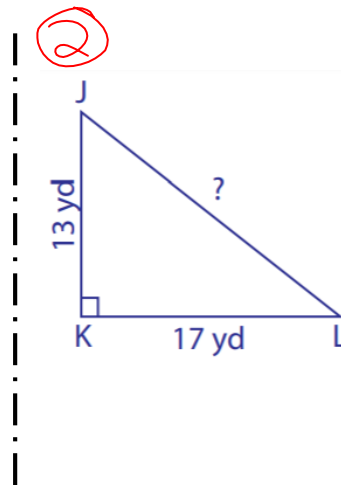
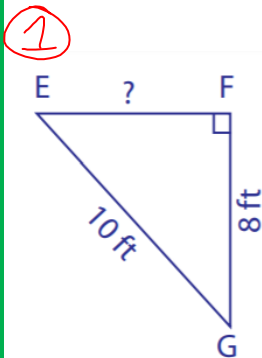
$$\begin{array}{r} 225 \\ -144 \\ \hline 81 \end{array} = X^2$$

$$\sqrt{81} = \sqrt{X^2}$$

$$9 = X$$

CODE GREEN

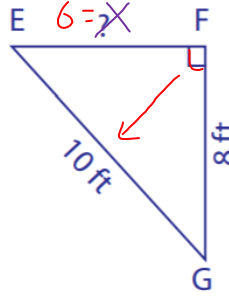
Solving for missing sides:



CODE RED – DO NOW

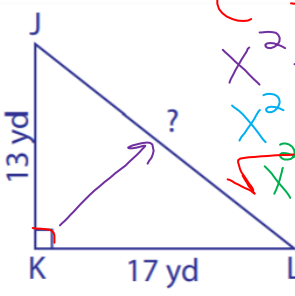
Solving for missing sides:

①



$C^2 = a^2 + b^2$
 $10^2 = 8^2 + x^2$
 $100 = 64 + x^2$
 $\begin{array}{r} 100 = 64 + x^2 \\ -64 \quad -64 \\ \hline 36 = x^2 \end{array}$
 $6 = x$

②

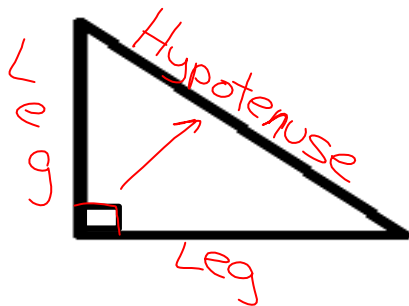


$C^2 = a^2 + b^2$
 $x^2 = 13^2 + 17^2$
 $x^2 = 169 + 289$
 $x^2 = 458$
 $x = 21.4$

CODE YELLOW

Vocabulary

Right Triangle – A triangle with one right angle



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The Pythagorean Theorem

$$c^2 = a^2 + b^2$$

CODE YELLOW

Which of the following sets of numbers could be the side lengths of a right triangle?

1) $\overbrace{9, 3, 8}^{11}$

$$c^2 = a^2 + b^2$$

$$9^2 = 3^2 + 8^2$$

$$81 = 9 + 64$$

$$81 > 73$$

2) $\overbrace{12, 13, 5}^{17}$

$$c^2 = a^2 + b^2$$

$$13^2 = 12^2 + 5^2$$

$$169 = 144 + 25$$

$$169 = 169 \checkmark$$

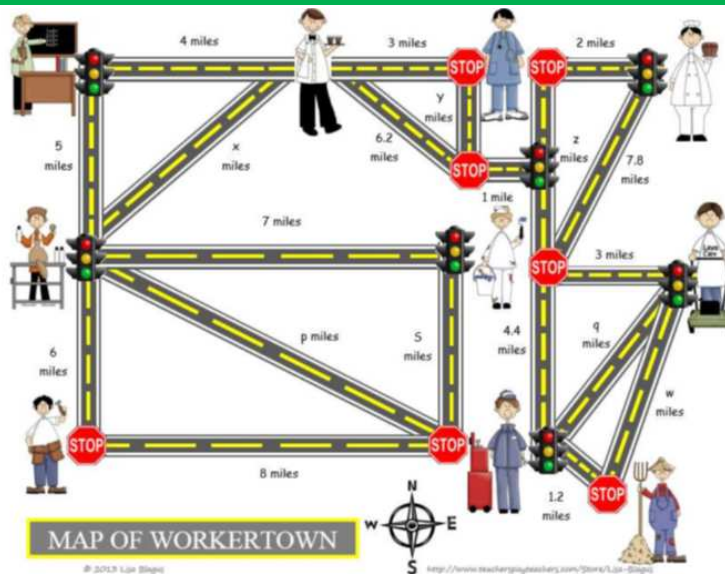


3) $\overbrace{4, 6, 11}^{10}$

10

Not a triangle

CODE GREEN



CODE RED – EXIT TICKET**Gridded Response**

Solve each exercise and enter your answer on the grid provided.
What is the value of x ?

